



Rethinking Computational Catalyst Searches with Alchemical Perturbation Density Functional Theory (APDFT)

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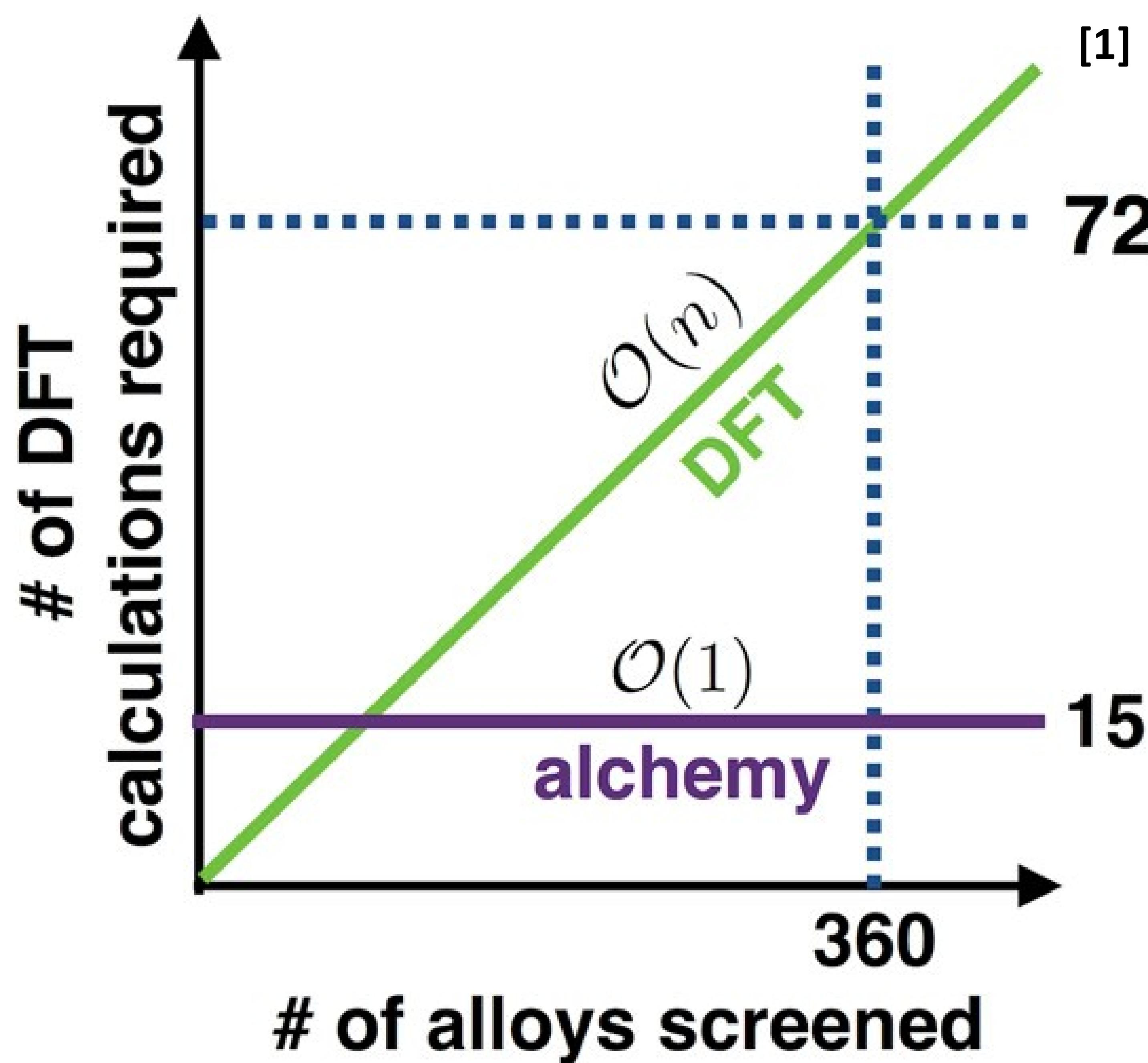
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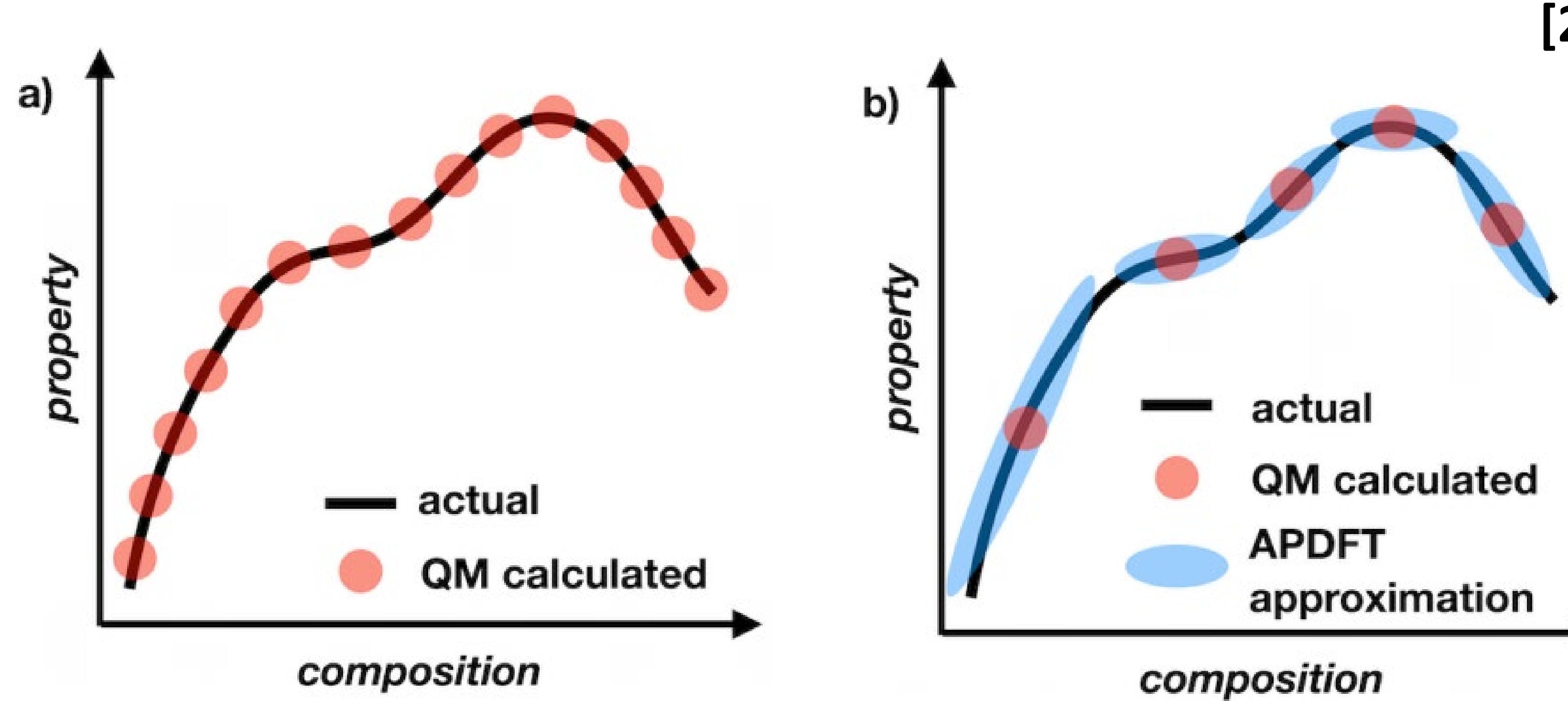


Background

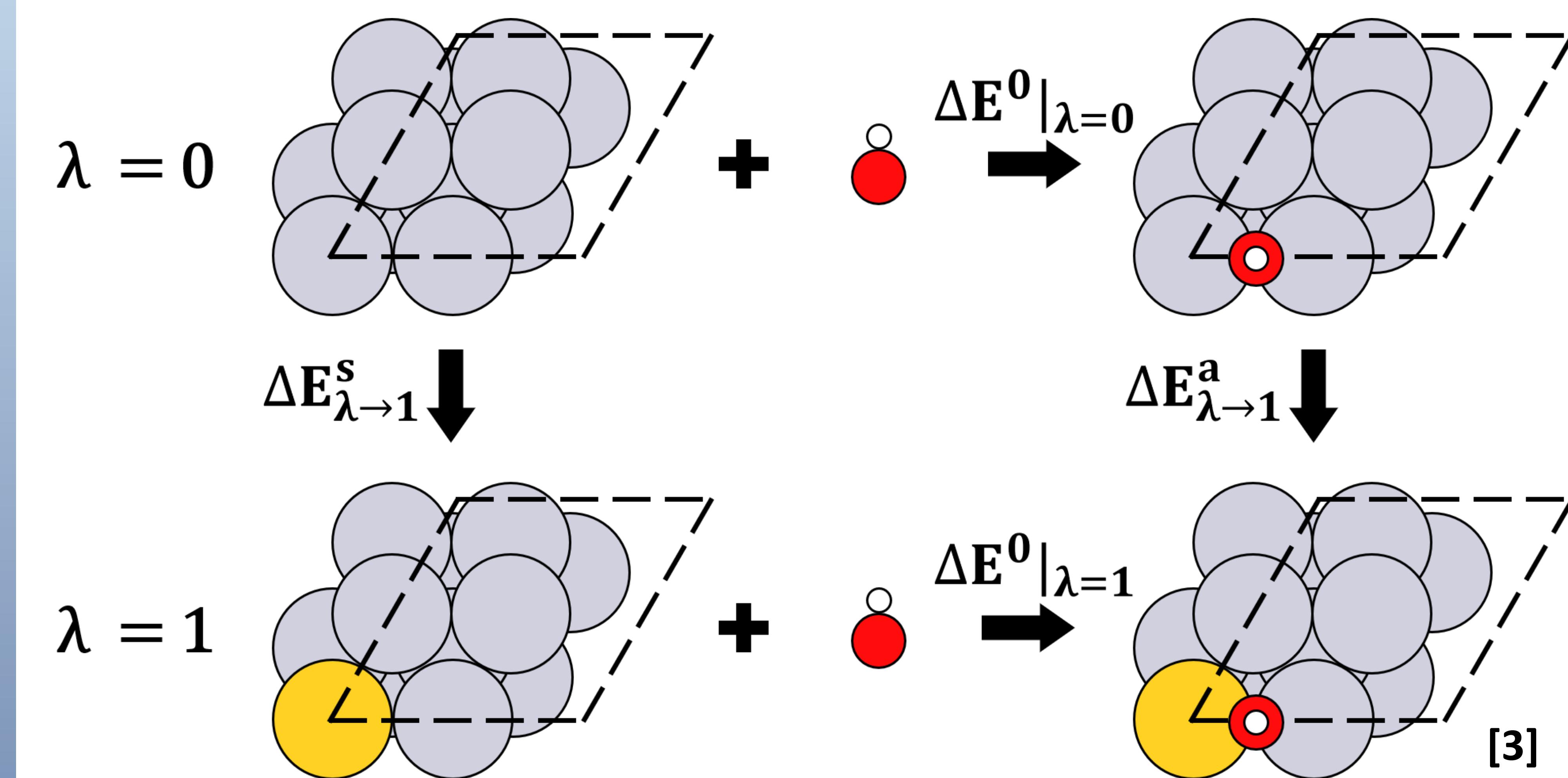
- Traditional Kohn-Sham density functional theory (KS-DFT) calculations increase the demand of computational resources.



- Alchemical Perturbation Density Functional Theory (APDFT) estimates catalyst descriptors with minimal computational cost.



Scheme for calculating BE with APDFT



Scheme for calculating BE with APDFT

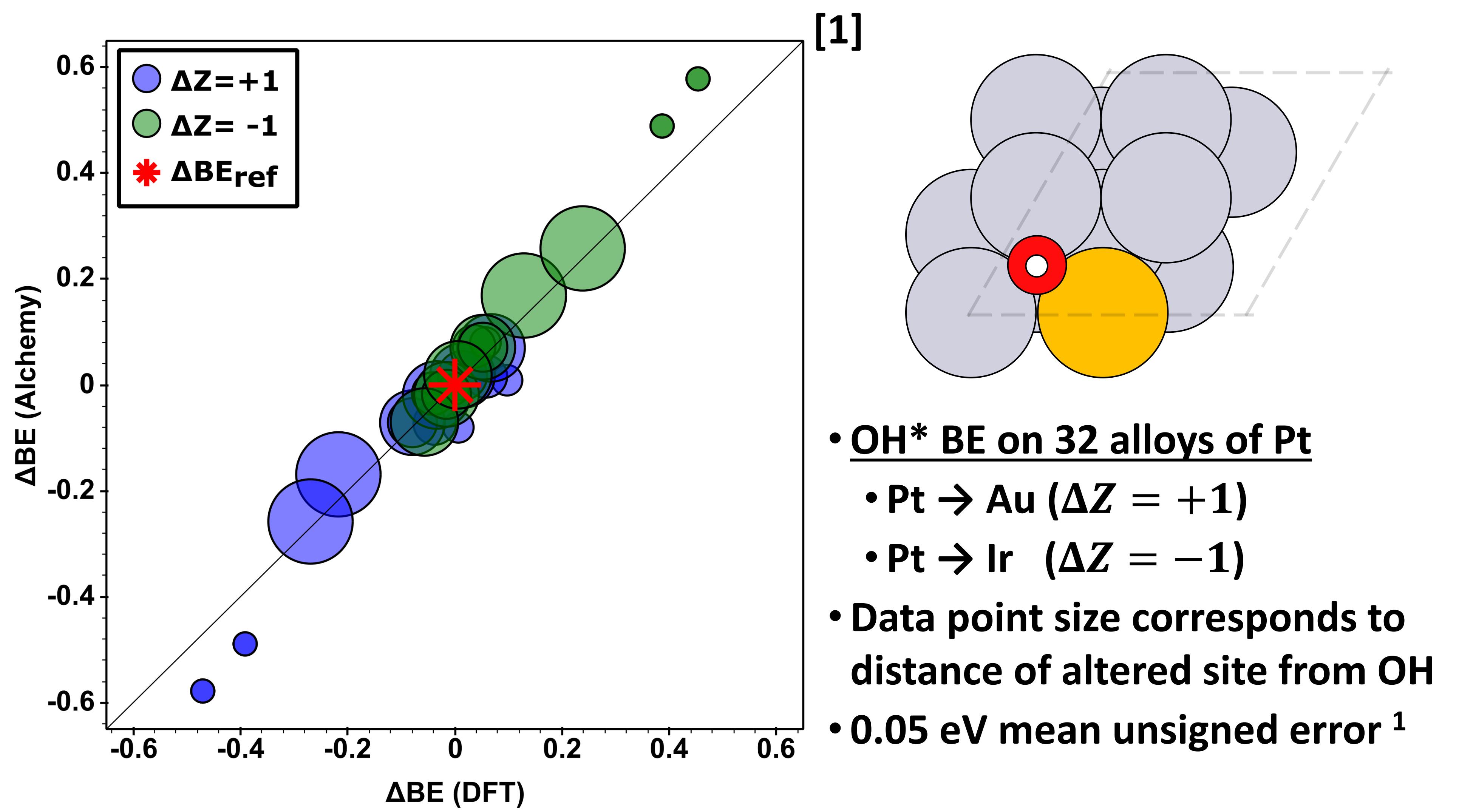
$$\begin{aligned}
 & \text{[3]} \\
 & \left[\begin{array}{c} \mu_1^a \\ \mu_2^a \\ \vdots \\ \mu_n^a \end{array} \right] - \left[\begin{array}{c} \mu_1^s \\ \mu_2^s \\ \vdots \\ \mu_n^s \end{array} \right] = \left[\begin{array}{c} \Delta\mu_1 \\ \Delta\mu_2 \\ \vdots \\ \Delta\mu_n \end{array} \right] \\
 & \left[\begin{array}{c} N_{Au} \\ N_{Pt} \\ \vdots \\ N_{Pt} \end{array} \right] - \left[\begin{array}{c} N_{Pt} \\ N_{Pt} \\ \vdots \\ N_{Pt} \end{array} \right] = \left[\begin{array}{c} 1 \\ 0 \\ \vdots \\ 0 \end{array} \right] \\
 & \partial_\lambda \Delta E^0 = \sum_I \Delta\mu_{nI} \partial_\lambda N_I = \left[\begin{array}{c} \Delta\mu_1 \\ \Delta\mu_2 \\ \vdots \\ \Delta\mu_n \end{array} \right] \cdot \left[\begin{array}{c} 1 \\ 0 \\ \vdots \\ 0 \end{array} \right] = \Delta BE_{alc}
 \end{aligned}$$

1. Karthikeyan Saravanan; John R. Kitchin; O. Anatole von Lilienfeld; John A. Keith; *J. Phys. Chem. Lett.* **2017**, 8, 5002-5007.

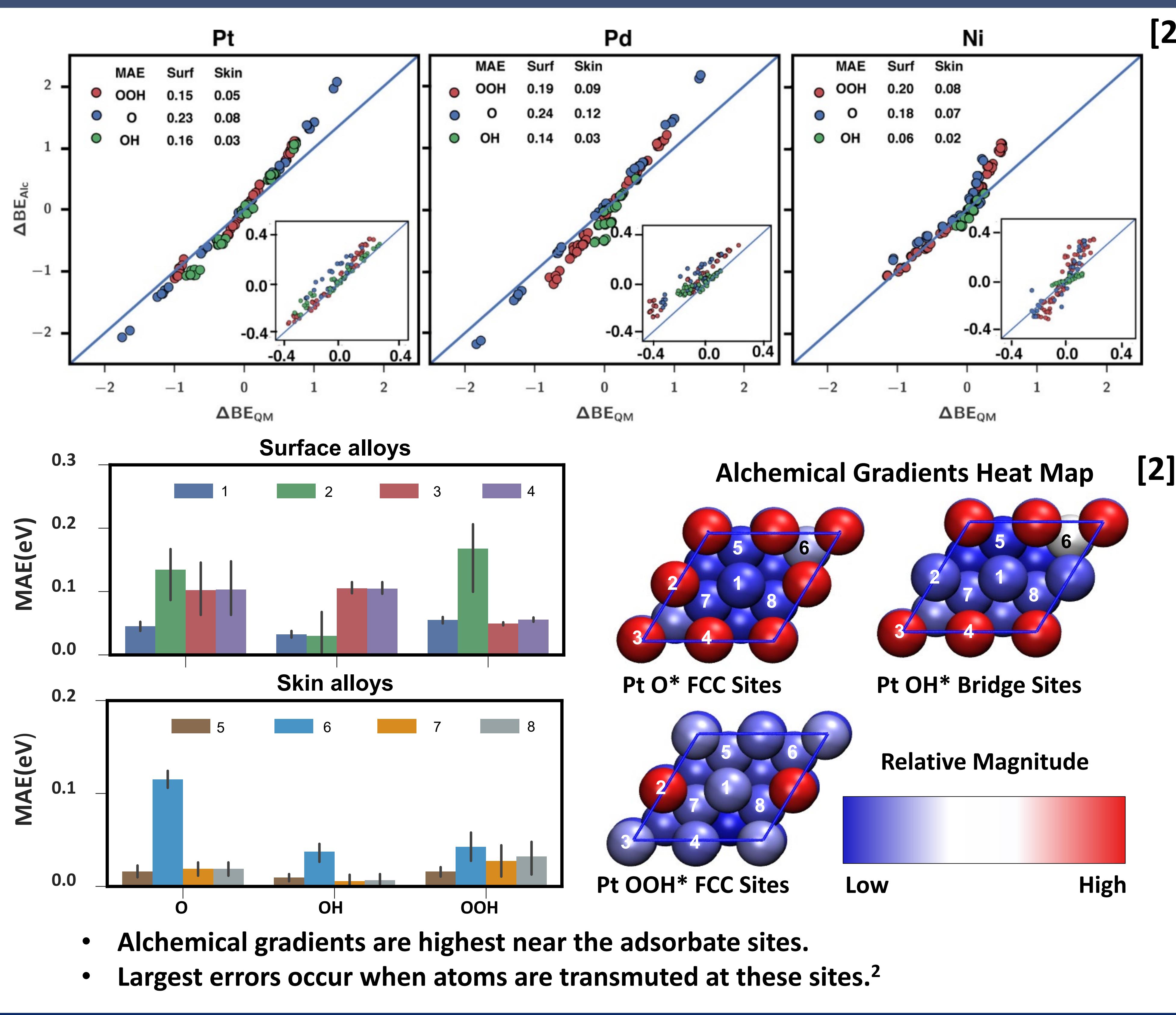
2. John A. Keith; *Electrochim. Soc. Interface*, **2020**, 29, 63

3. Charles D. Griego; John R. Kitchin; John A. Keith; *Int. J. Quantum. Chem.* **2020**, 121:e26389

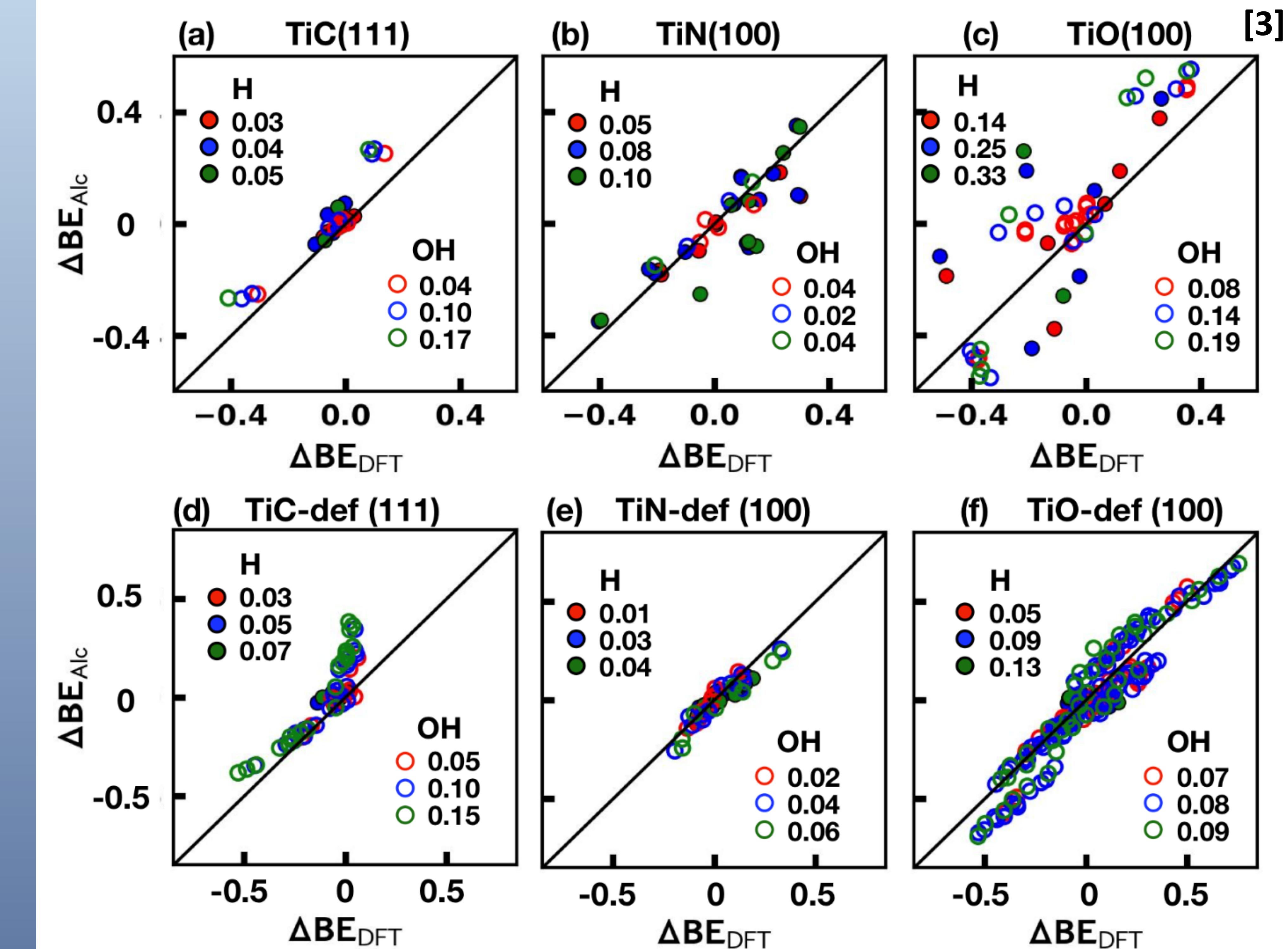
Binding Energy Predictions: Example Case ¹



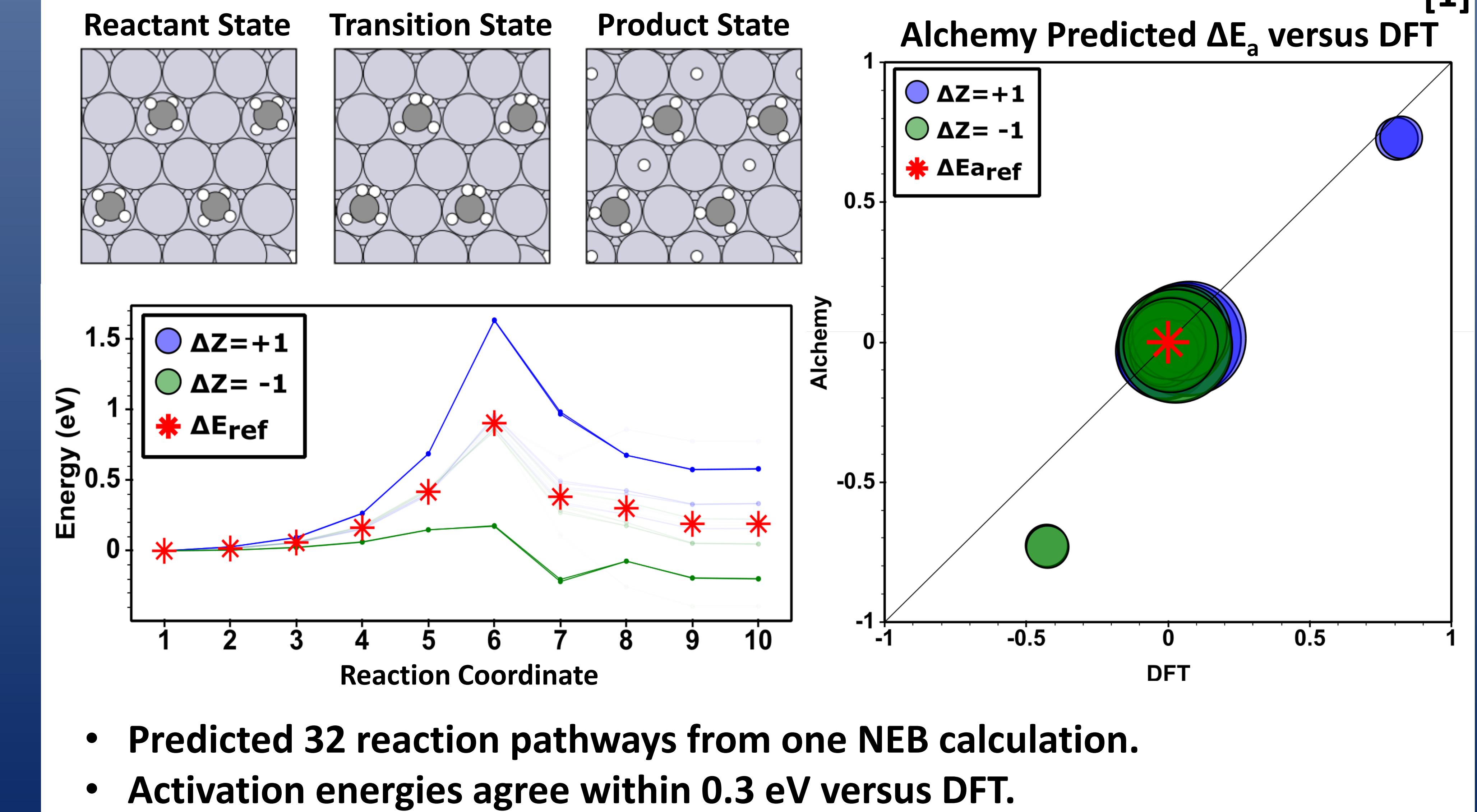
BE Predictions: Pt, Pd, and Ni Alloys ²



BE Predictions: TiC, TiN, and TiO Materials ³



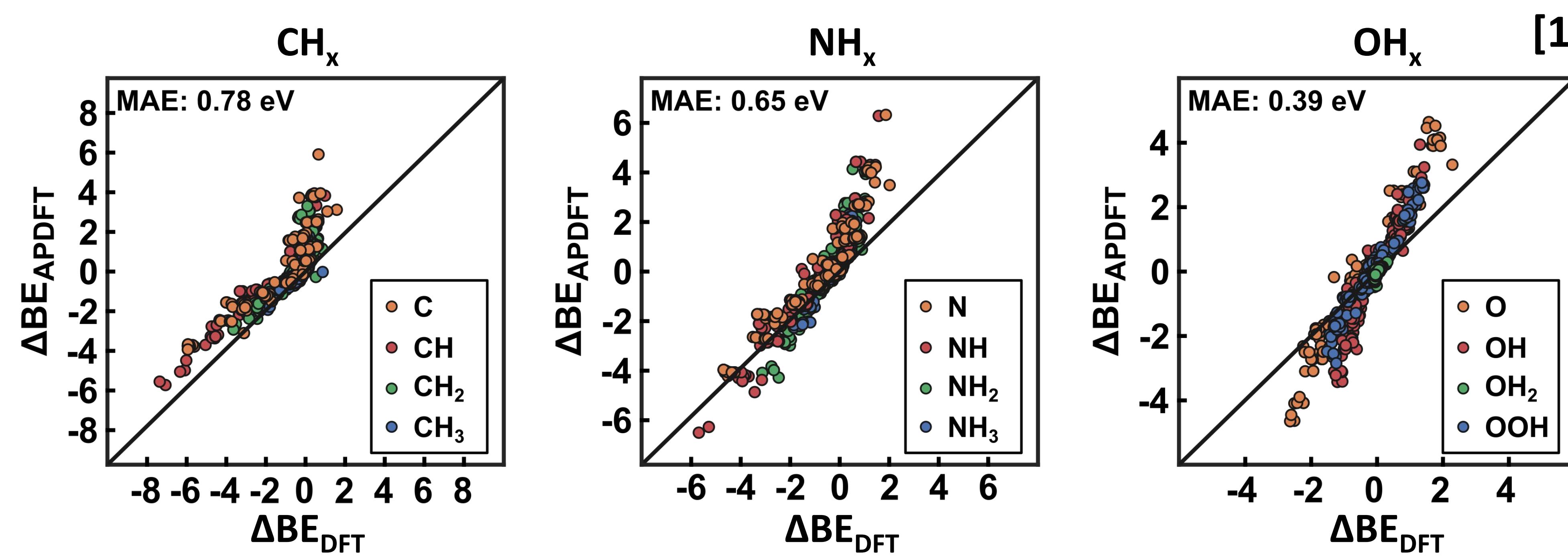
Reaction Pathways and Activation Energy ¹



- Charles D. Griego; John R. Kitchin; John A. Keith; *Int. J. Quantum. Chem.* **2020**, 121:e26389
- Karthikeyan Saravanan; John R. Kitchin; O. Anatole von Lilienfeld; John A. Keith; *J. Phys. Chem. Lett.* **2017**, 8, 5002-5007.

- Charles D. Griego; Karthikeyan Saravanan; John A. Keith; *Adv. Theory Sim.* **2019**, 2: 1800142

Identifying Shortcomings with APDFT¹

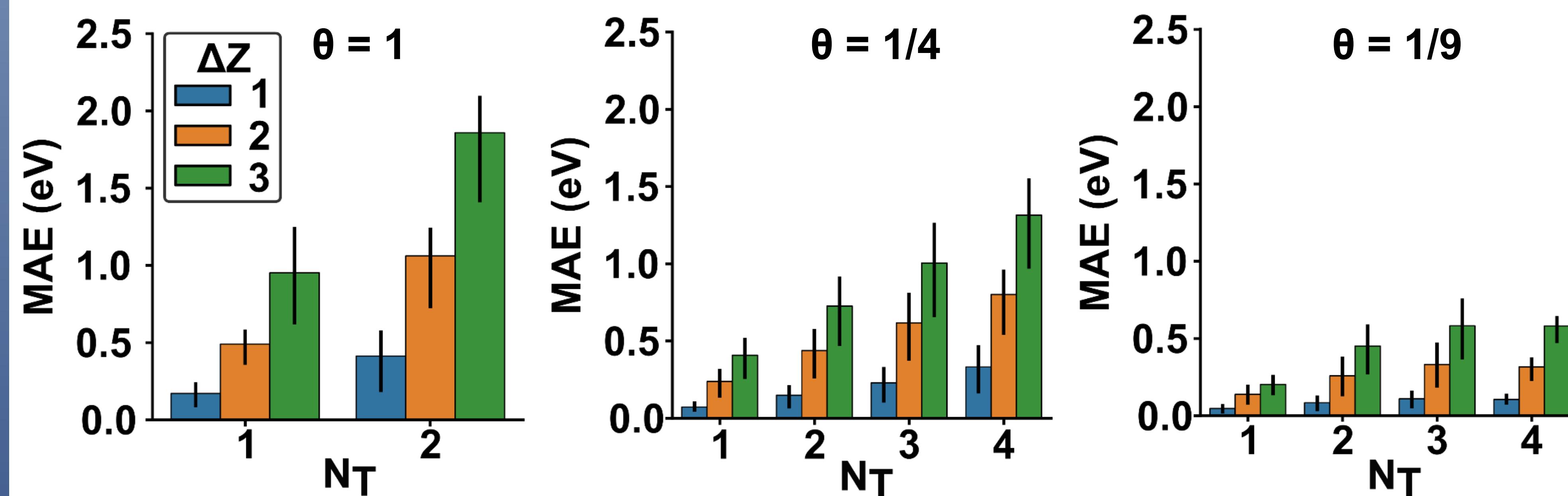


Adsorbates on Pt alloys:
 • CH_x, NH_x, OH_x (x = 0-3)
 • Coverage $\theta = 1, 1/4, 1/9$

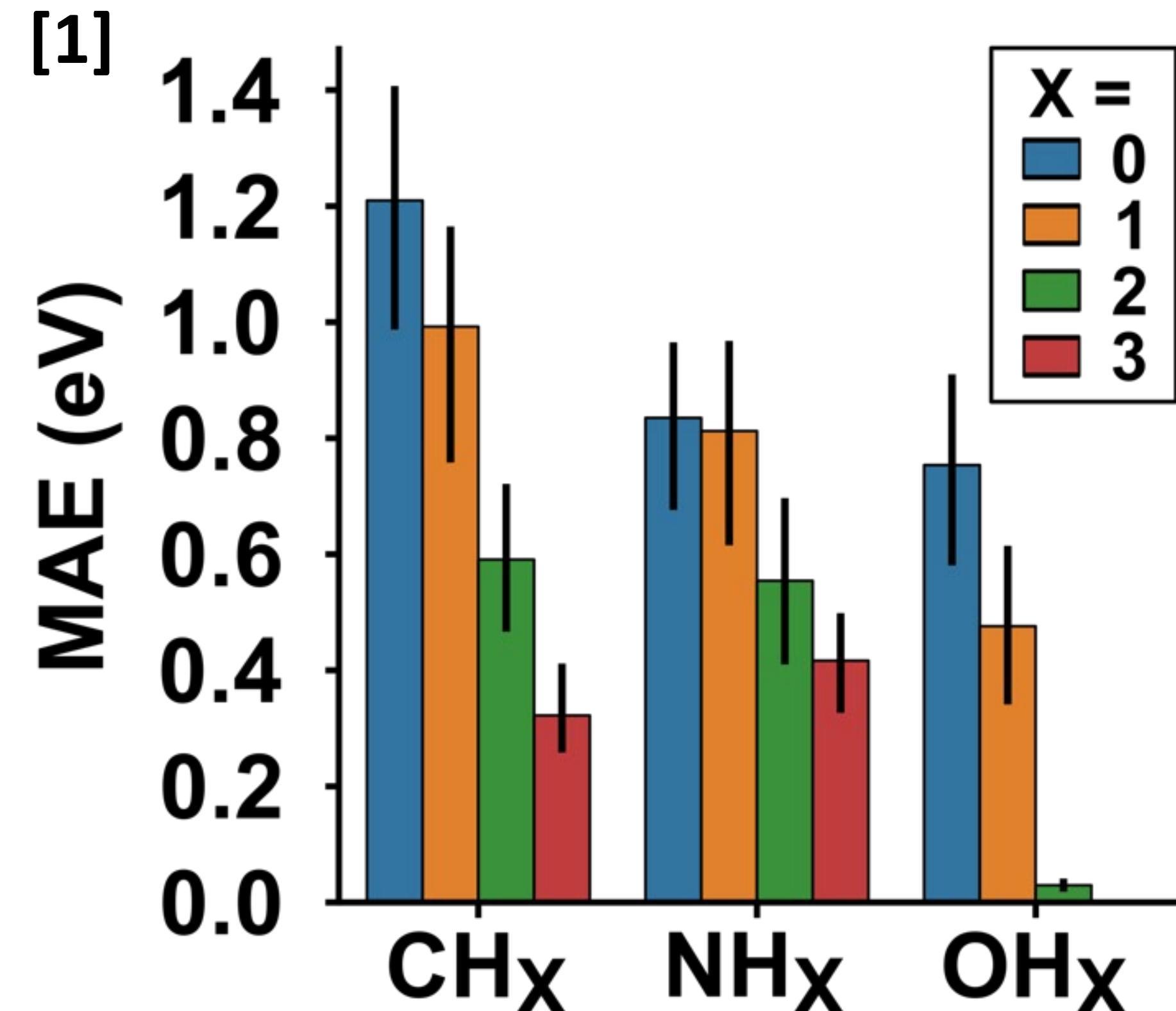
Alloy variations:
 • # of transmutations $N_T = 1, 2, 3$, or 4
 • Nuclear charge change $\Delta Z = 1, 2$, or 3

Breaking Down Sources of Error¹

APDFT errors sorted by N_T , ΔZ , and θ [1]



APDFT errors by adsorbate type



Overall Observations:¹

- Errors increase with N_T and ΔZ
- Errors increase with θ
- Errors decrease with hydrogenation of the central atom in the adsorbate

Correcting APDFT with Machine Learning¹

ML Workflow

[1]
Input: Define a hypothetical alloy by making transmutations to a reference catalyst surface

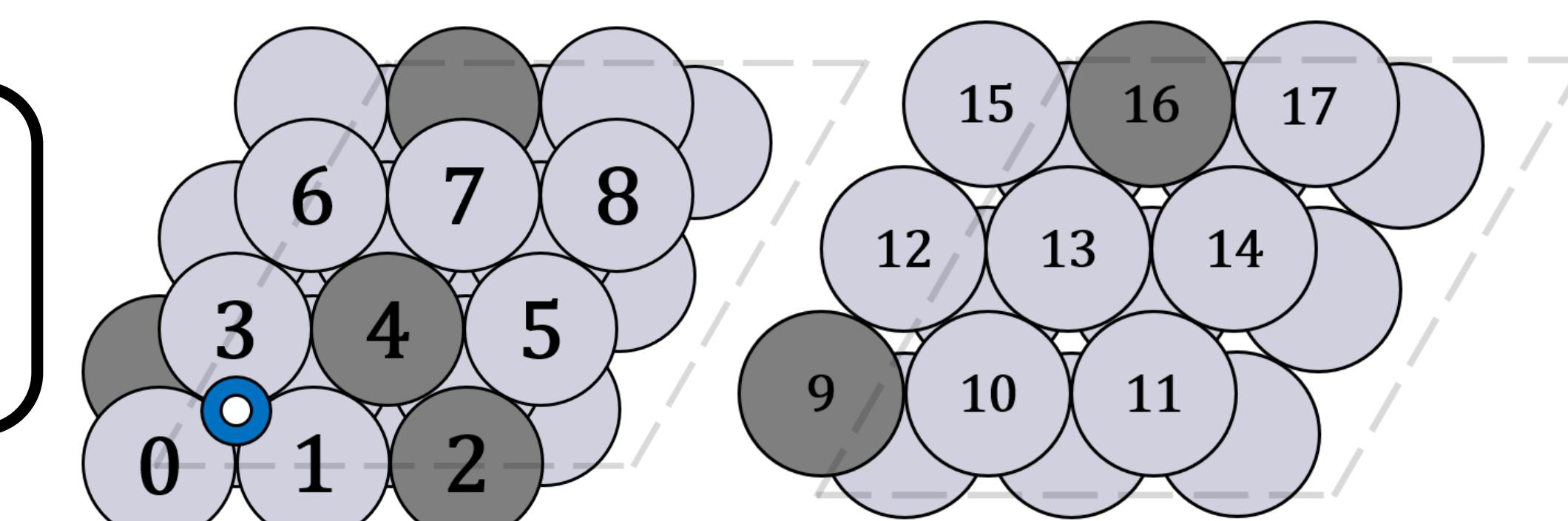
Fingerprinting: Label transmuted sites as 1 and remaining sites 0

Feature Vector Construction: Record dopant fingerprints, ΔZ , N_T , adsorbate type, θ , and dopant in an array

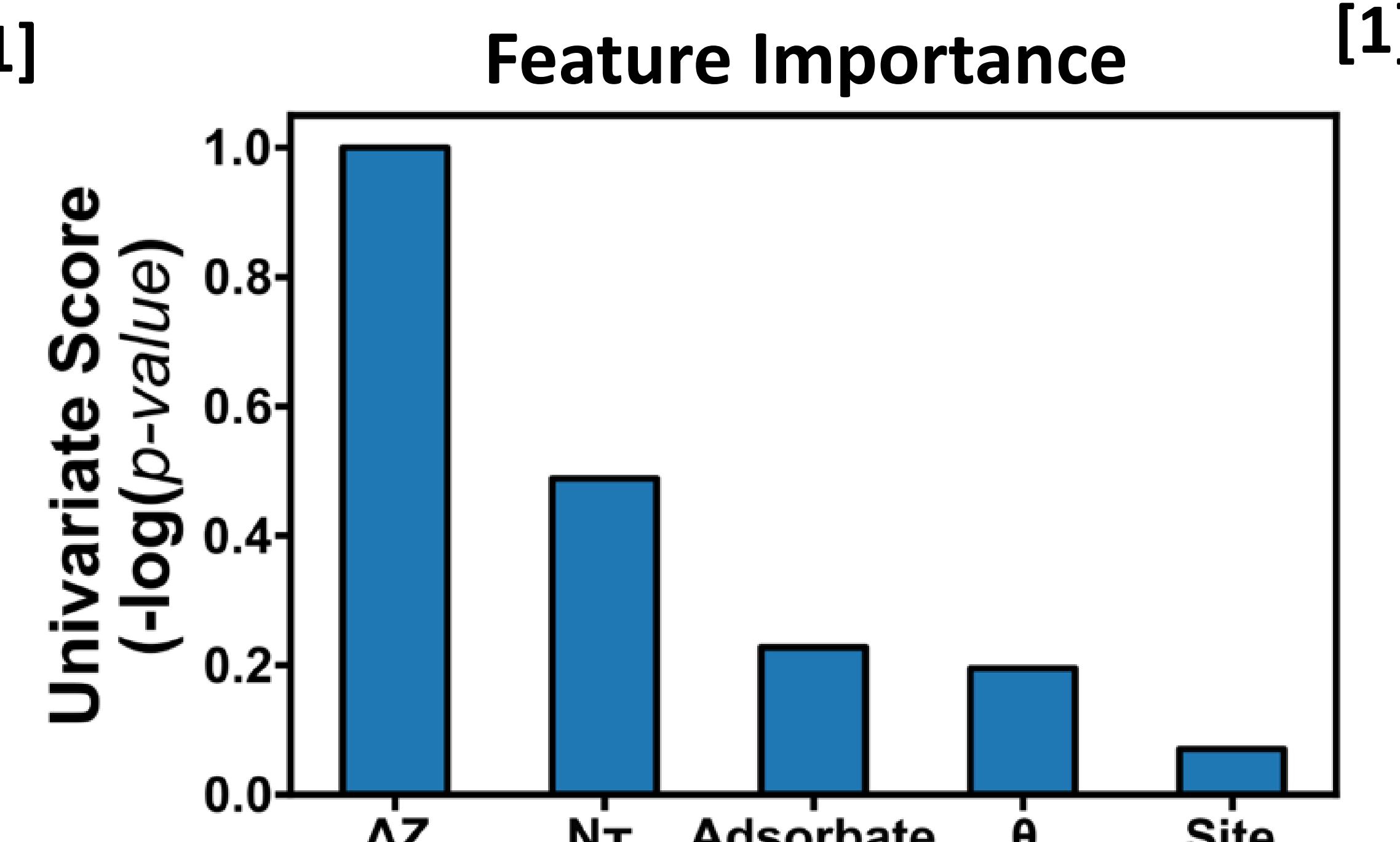
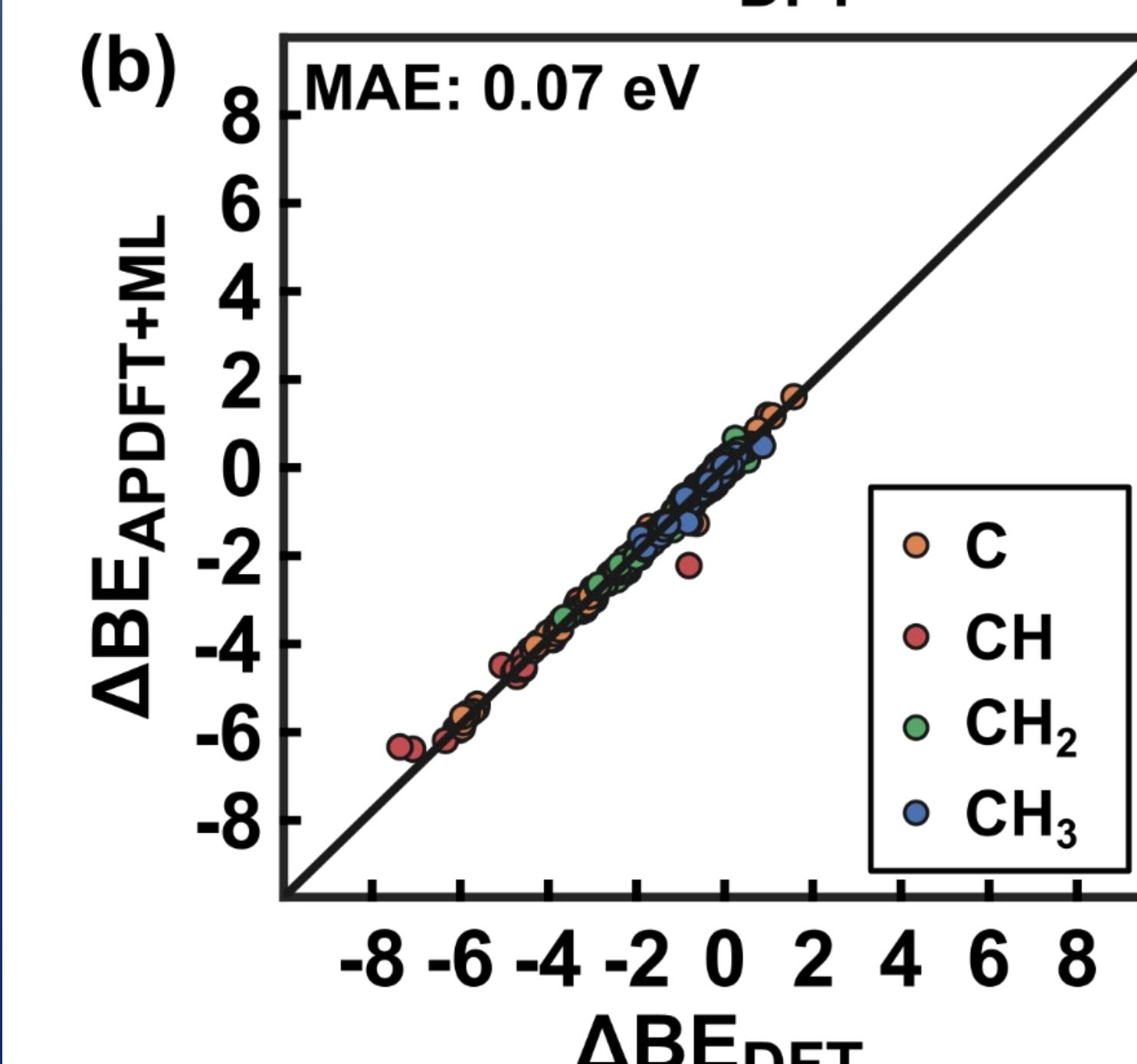
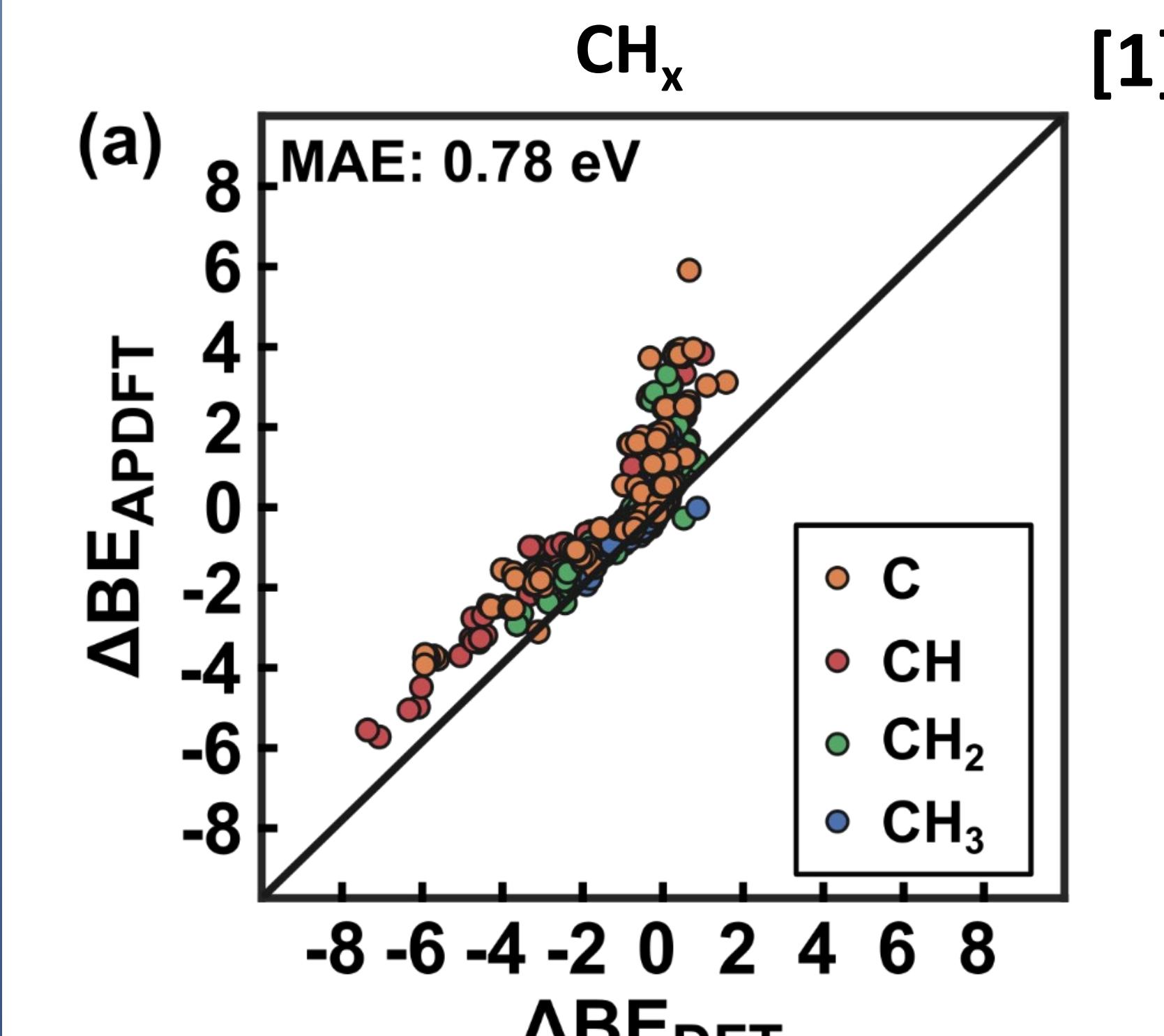
ML Model: Predict error between APDFT and DFT (Error_{ML})

ML-corrected APDFT BE prediction:

$$\text{BE}_{\text{APDFT+ML}} = \text{BE}_{\text{APDFT}} + \text{Error}_{\text{ML}}$$



[0 0 1 0 1 0 0 0 0
1 0 0 0 0 0 0 1 0]



- APDFT errors are predicted with support vector regression models
- MAE reduced by an order of magnitude (dataset of CH_x adsorbates)
- ΔZ and N_T have the greatest influence on the model predictions

1. Charles D. Griego; Lingyan Zhao; Karthikeyan Saravanan; John A. Keith; *AIChE J.* 2020, 66:e17041